

# Tardiness Bounds for Fixed-Priority Global Scheduling without Intra-Task Precedence Constraints

Sergey Voronov, James H. Anderson, Kecheng Yang

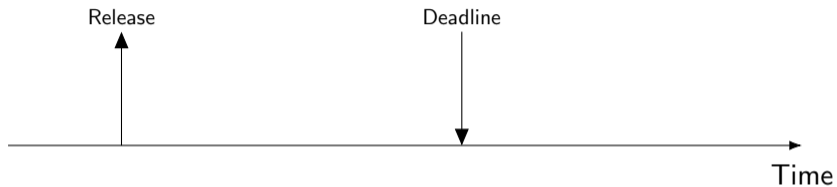
The University of North Carolina at Chapel Hill  
Department of Computer Science

October 10, 2018

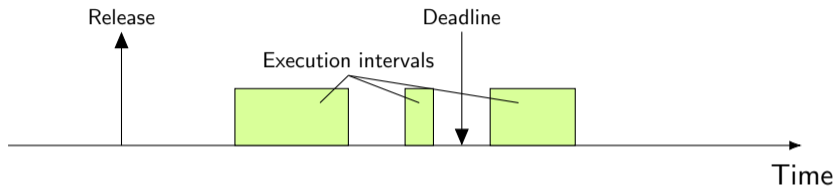
# Soft Real-Time (SRT)



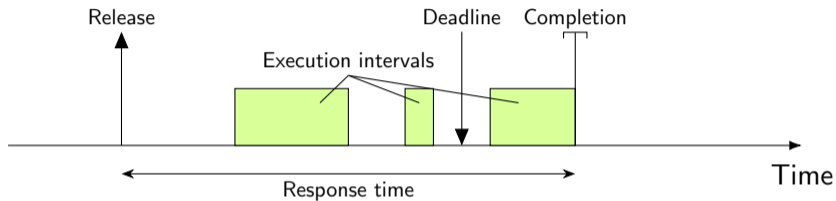
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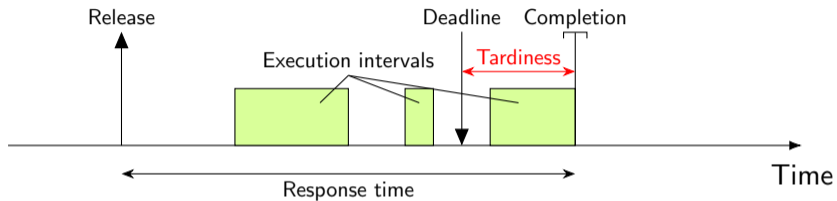
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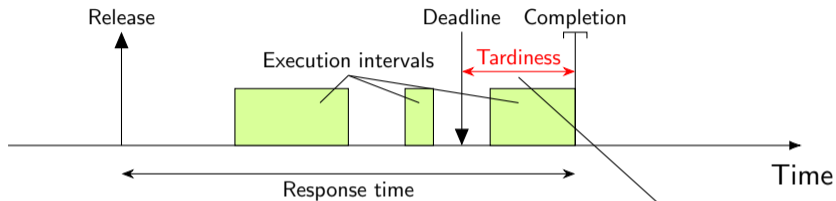
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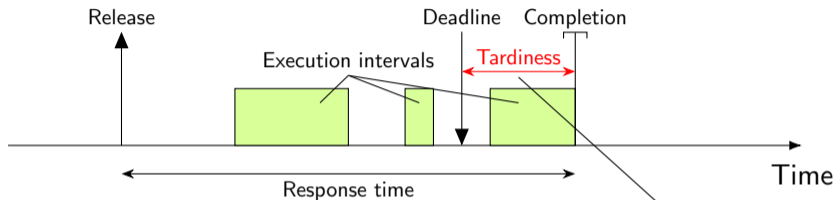


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Task tardiness:  
 $\max_{jobs}(\text{job tardiness})$

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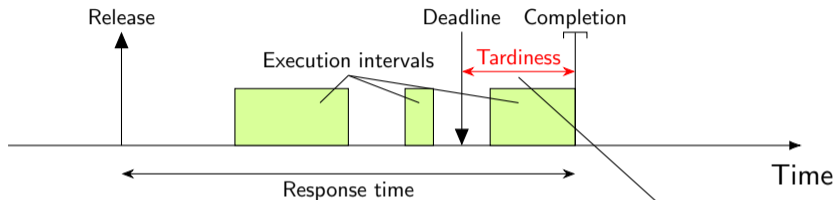


Approach | Goal

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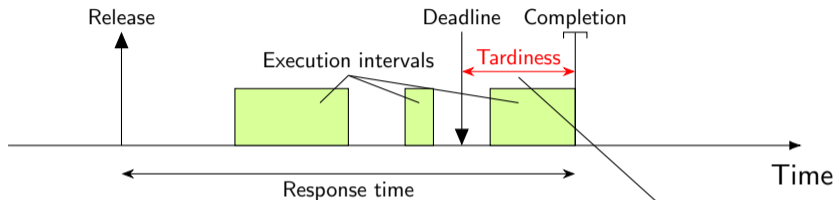
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Hard Real-Time	no tardiness at all

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Approach	Goal
Hard Real-Time	no tardiness at all
Soft Real-Time	bounded tardiness for every task

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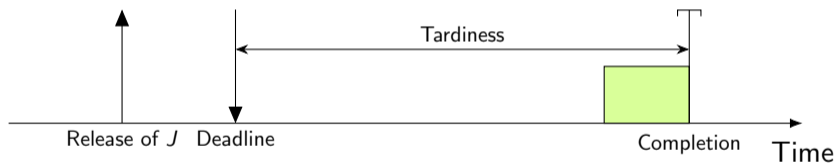
# Outline

- Review of G-EDF SRT-optimality proof
- G-FP and SRT-optimality
- Sporadic task model generalization: NPC-sporadic
- Key idea of G-FP-optimality proof under the generalized model

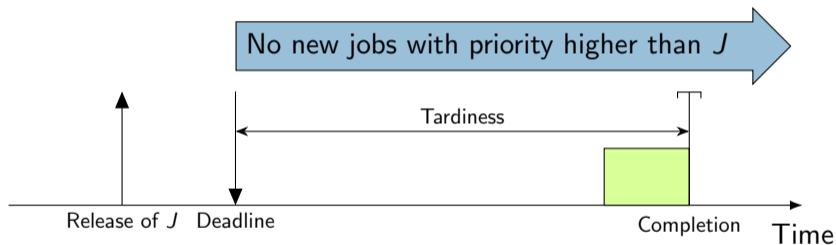
Main result:

Global Fixed Priority scheduling is SRT-optimal under the NPC-sporadic task model.

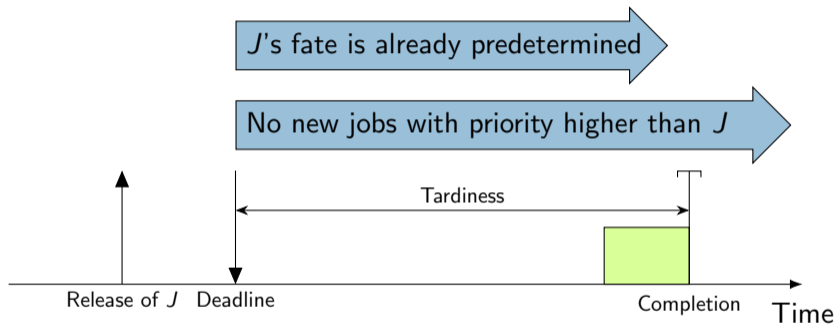
# G-EDF Soft Real-Time Optimality



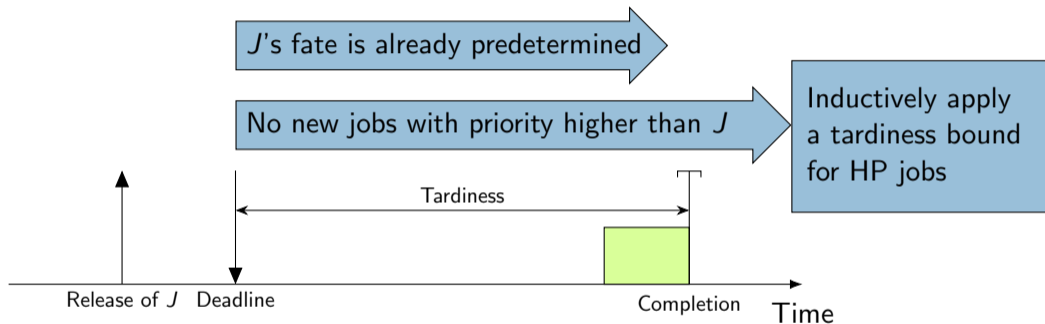
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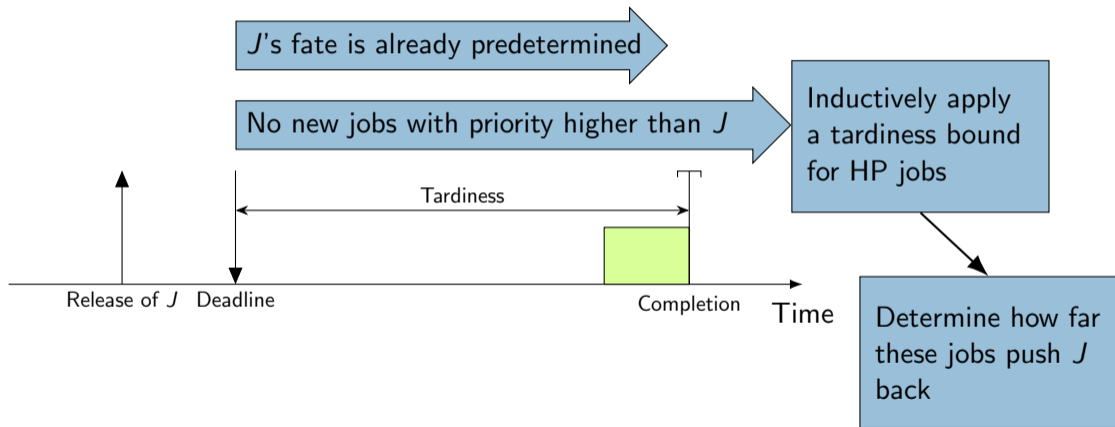
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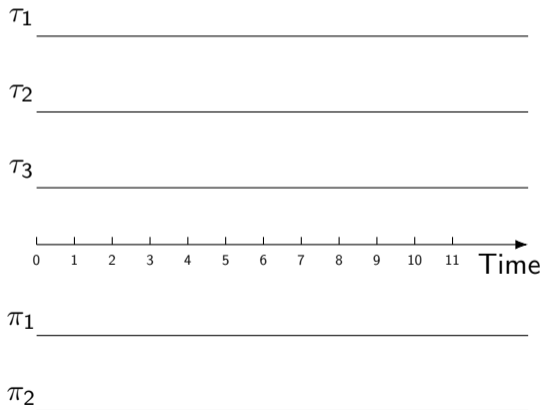
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multiprocessor with two unit-speed cores  $(\pi_1, \pi_2)$

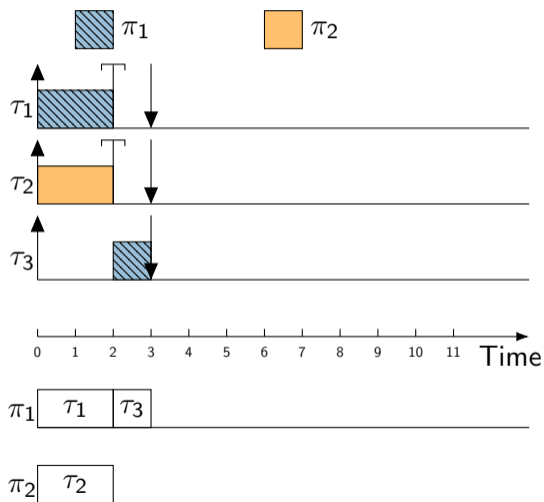


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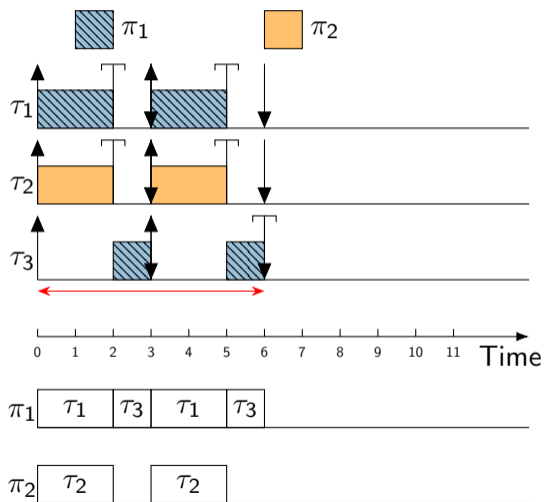


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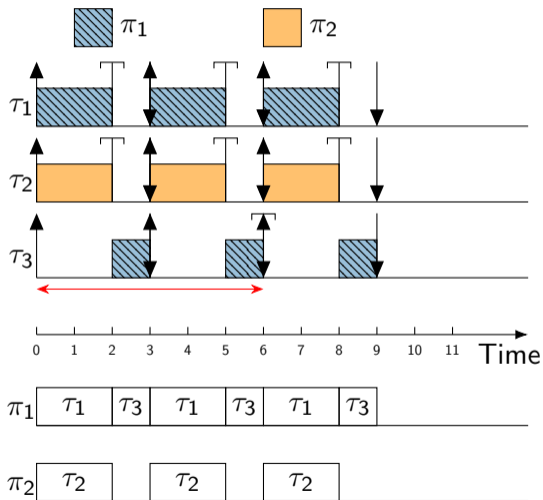


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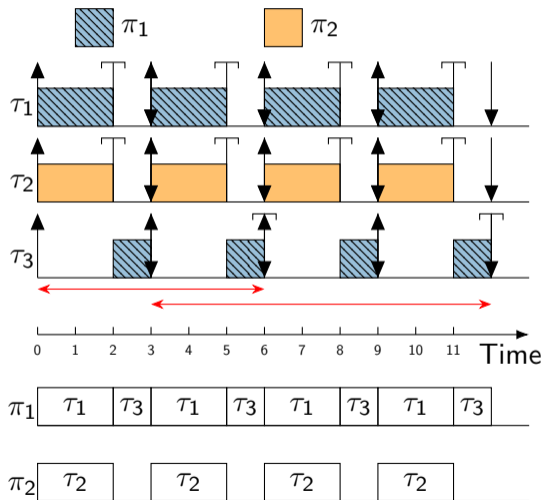


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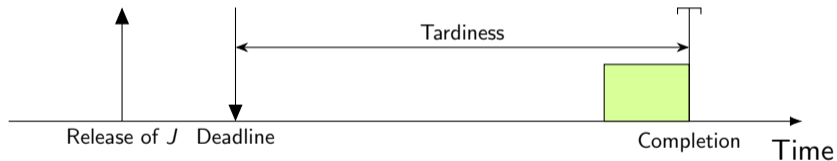
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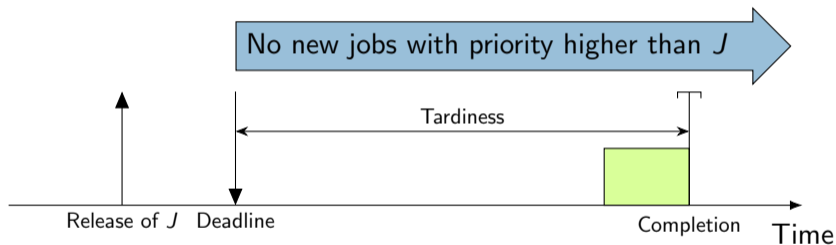




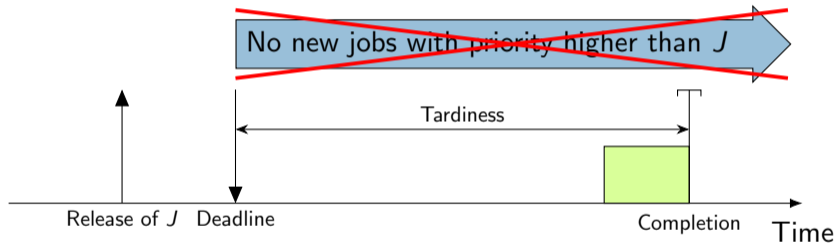
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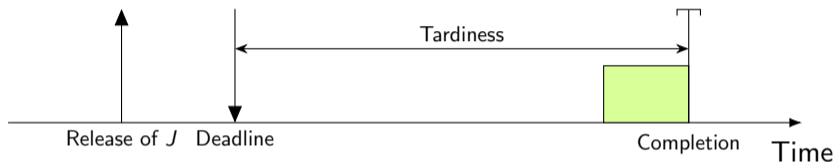
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- Industry interest: Huawei cell base stations

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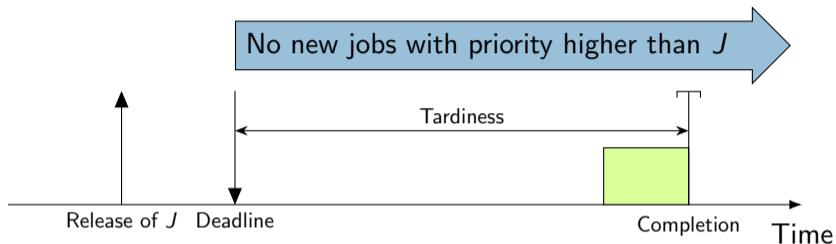
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# G-EDF under NPC-Sporadic Task Model



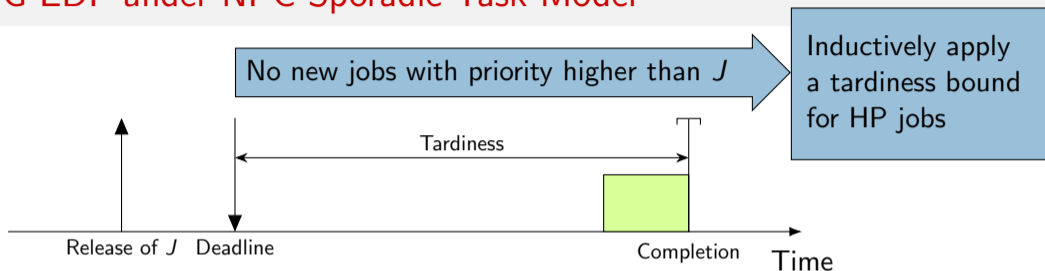
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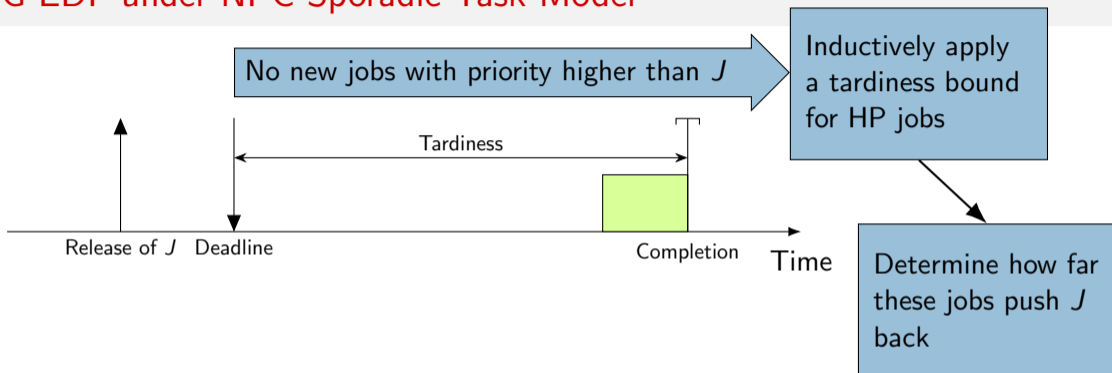
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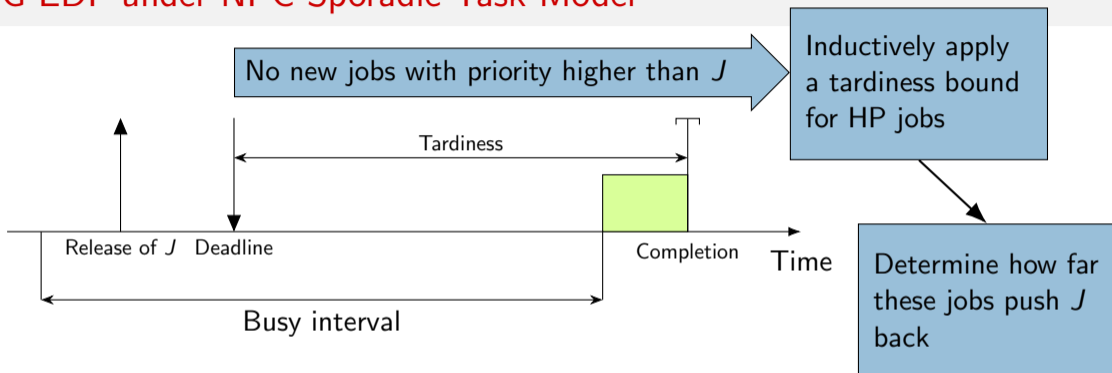
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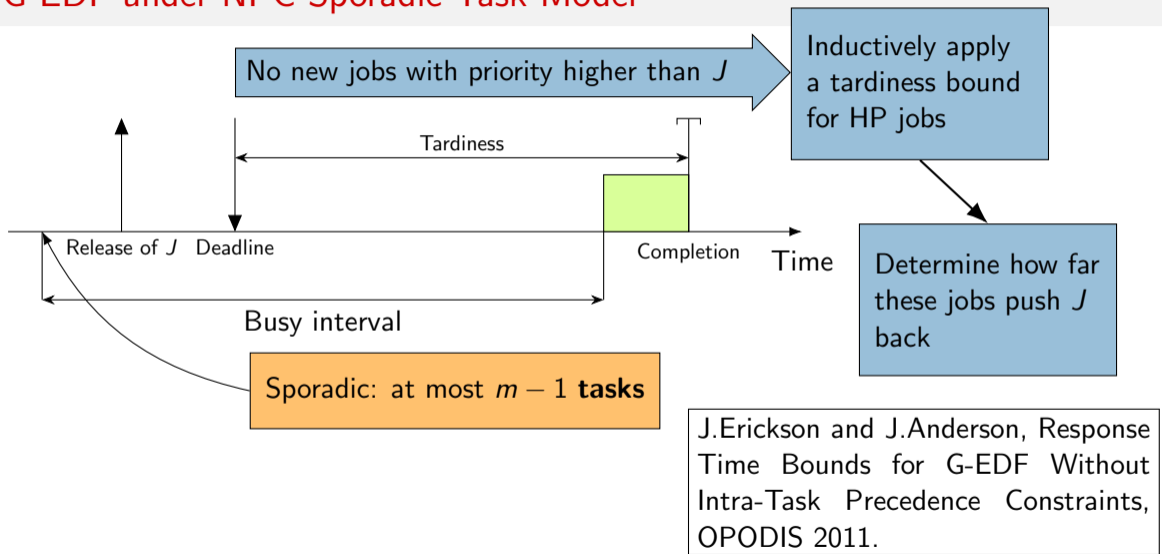
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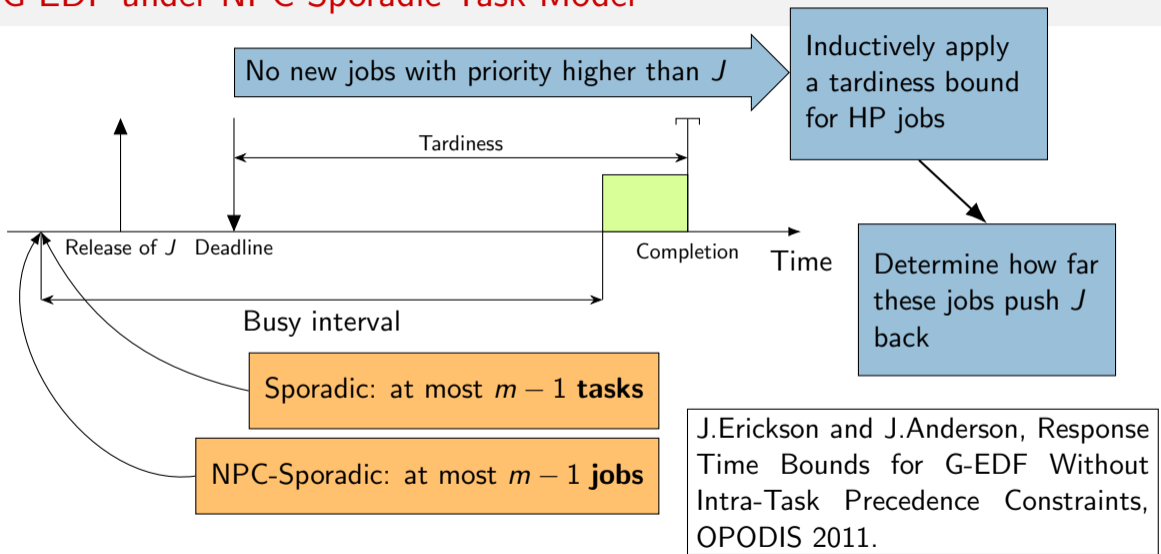
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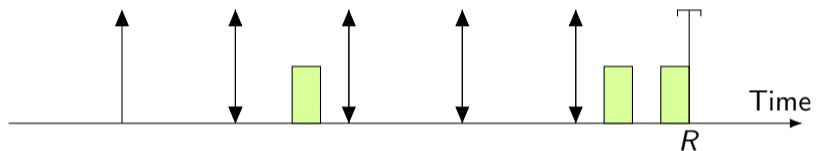
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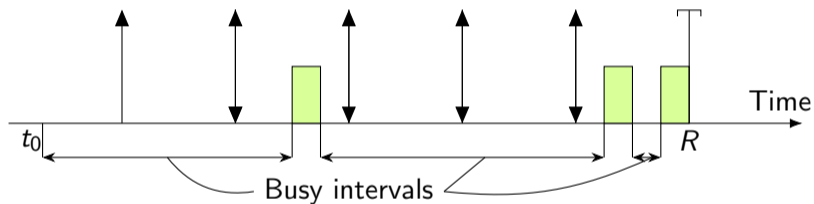
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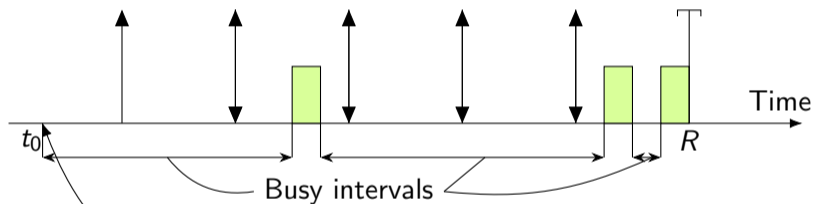
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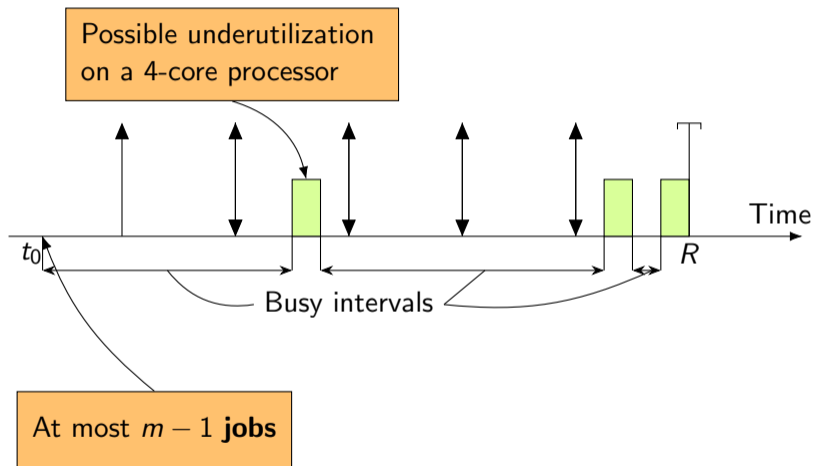


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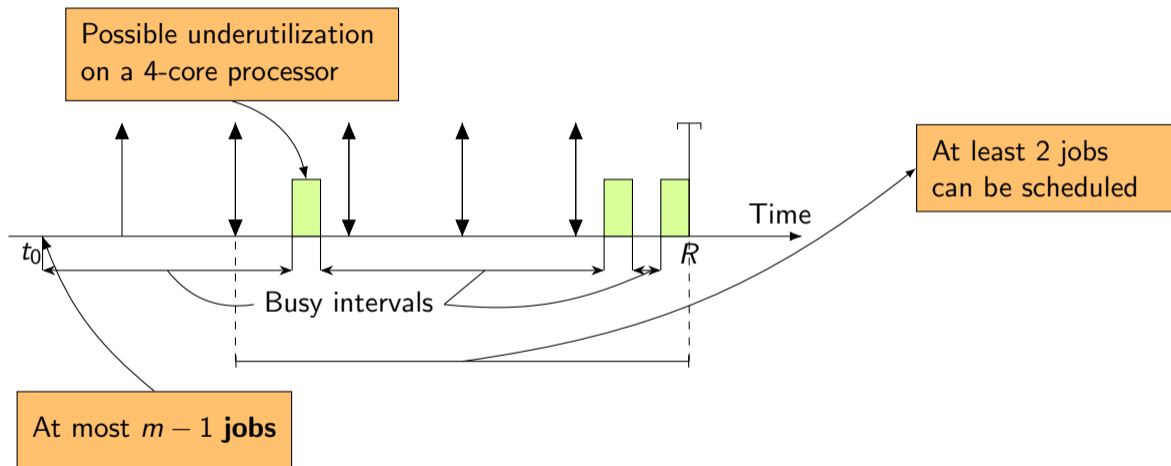


At most  $m - 1$  jobs

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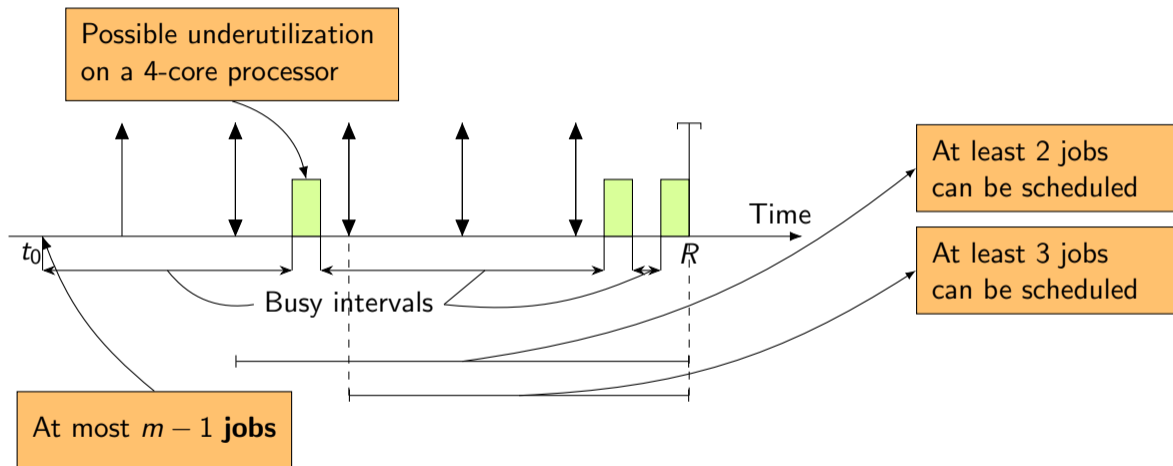


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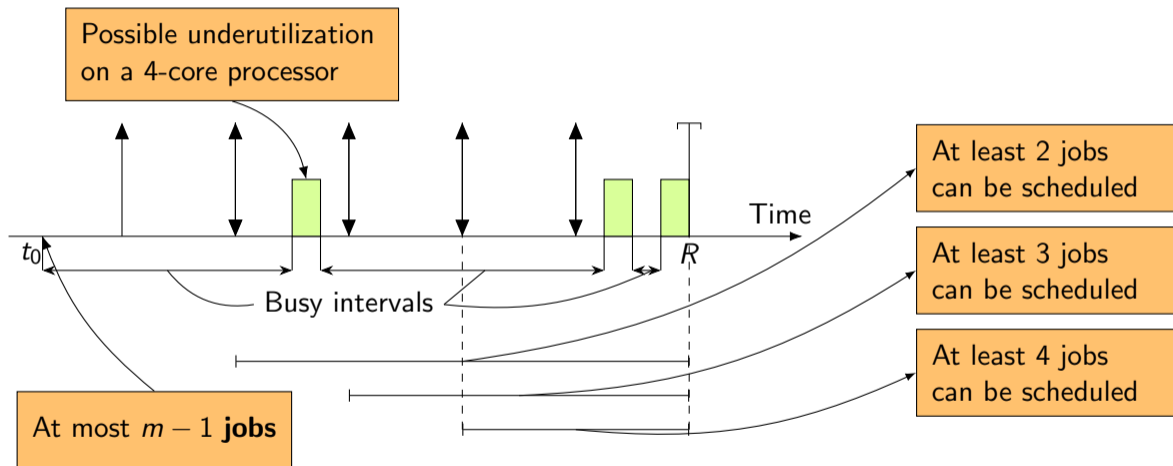




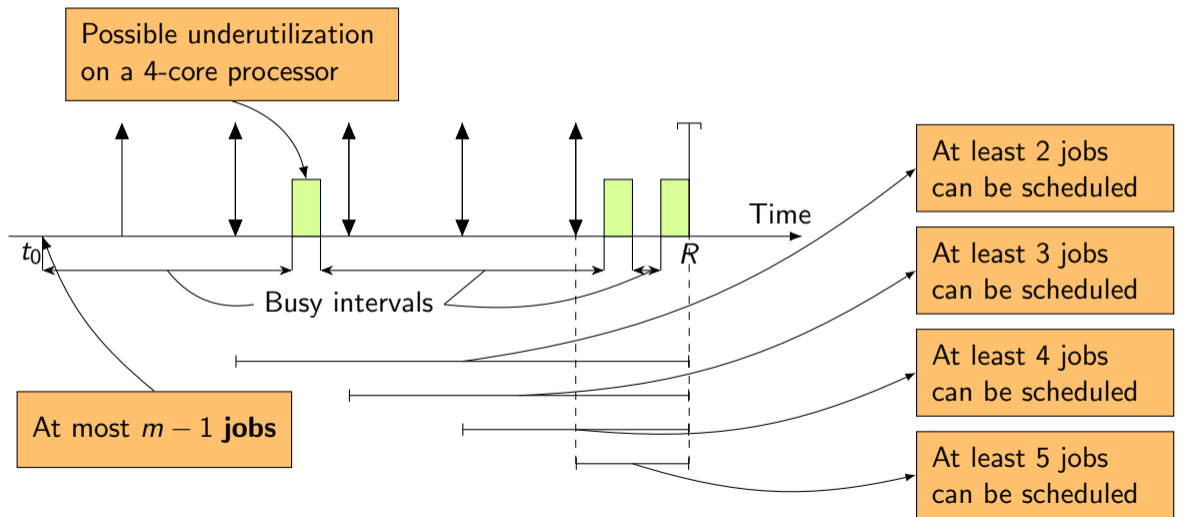
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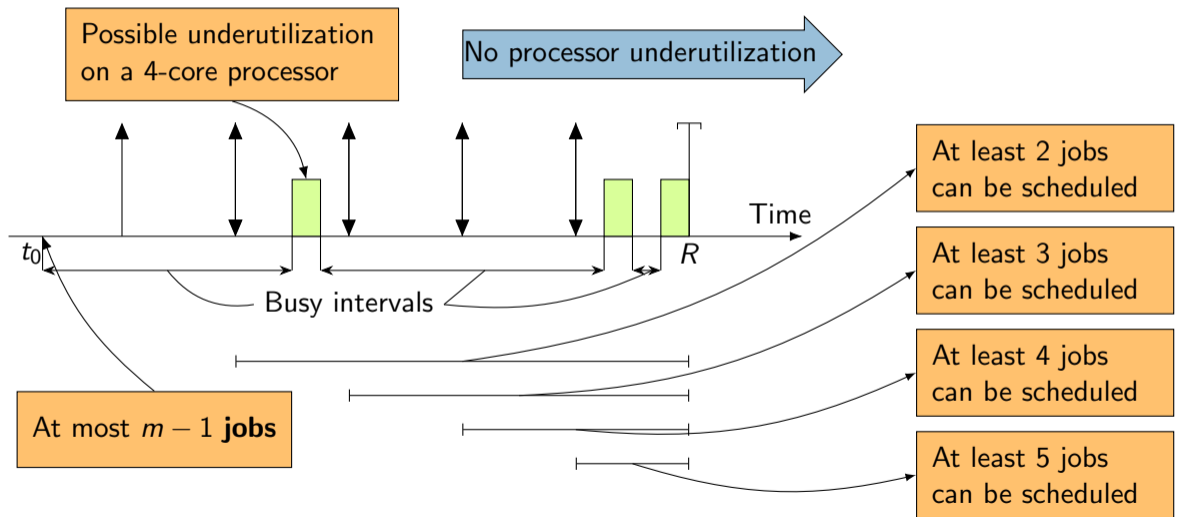
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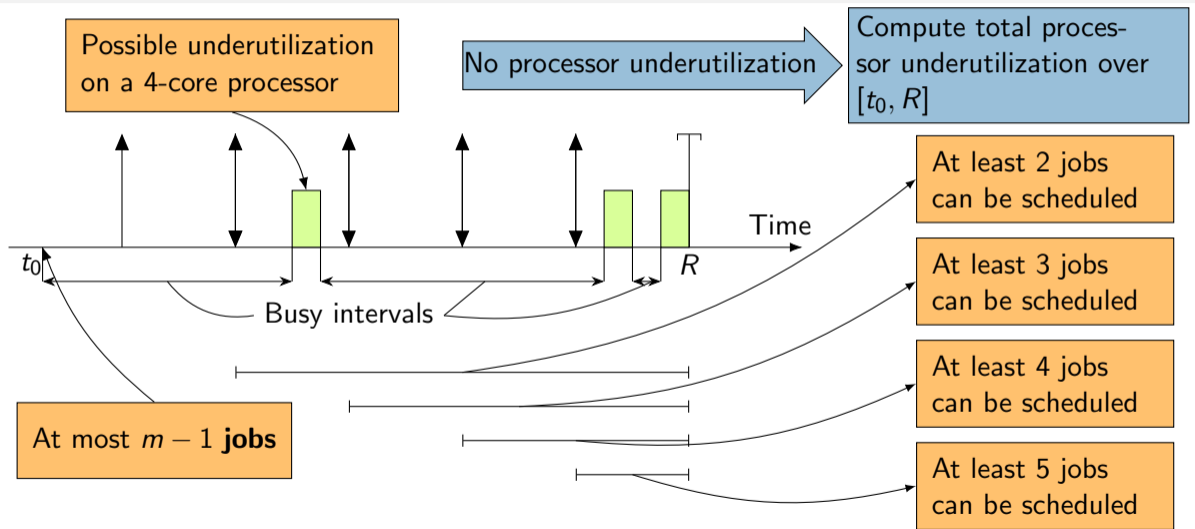
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- Asymptotically optimal

Prior work: J.Erickson and J.Anderson,  
Response Time Bounds for G-EDF Without Intra-Task Precedence Constraints,  
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# Experiments

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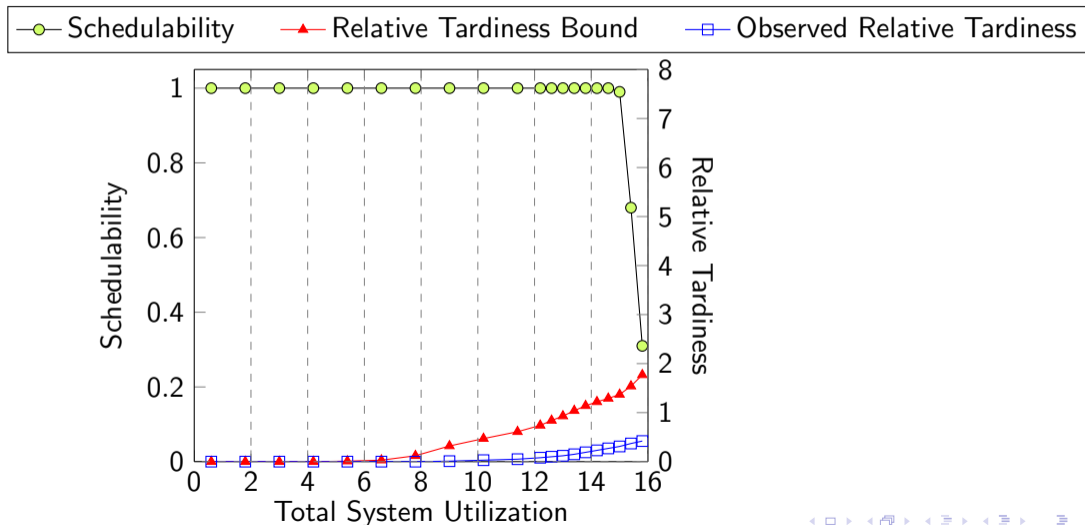
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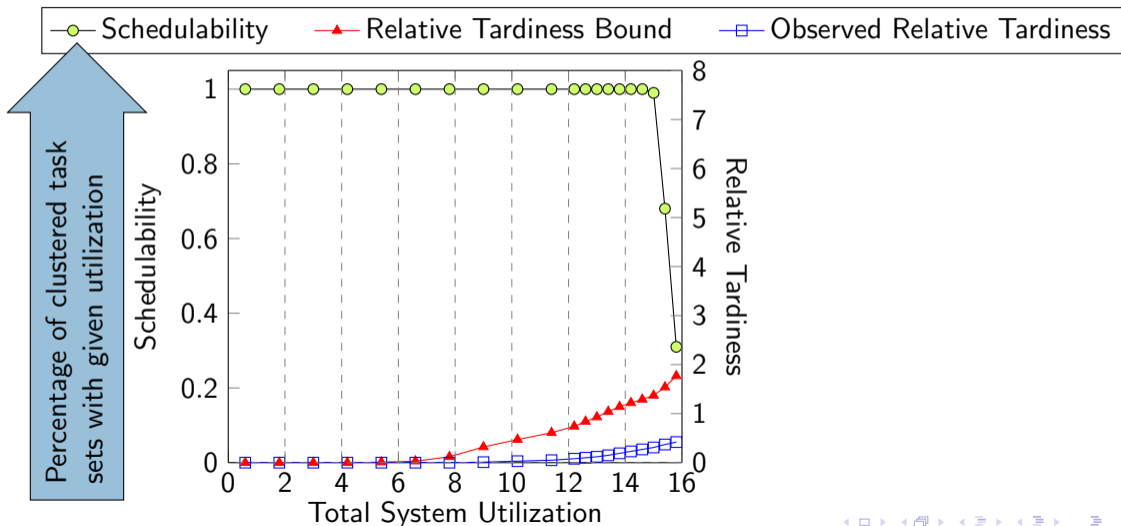
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- Use only bin packing heuristics
- Get smaller tardiness bounds

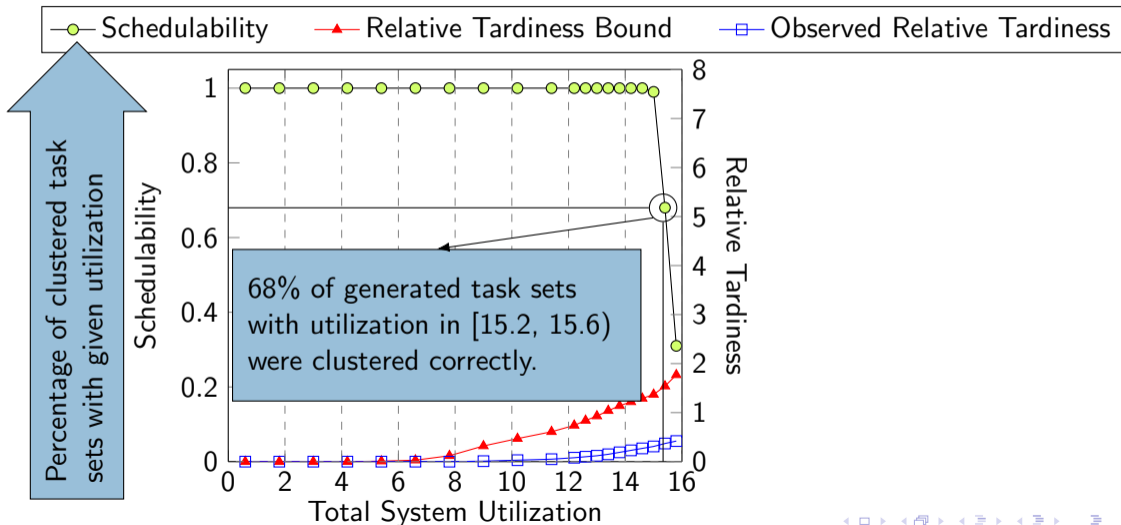
# Experiments: Sample Plot



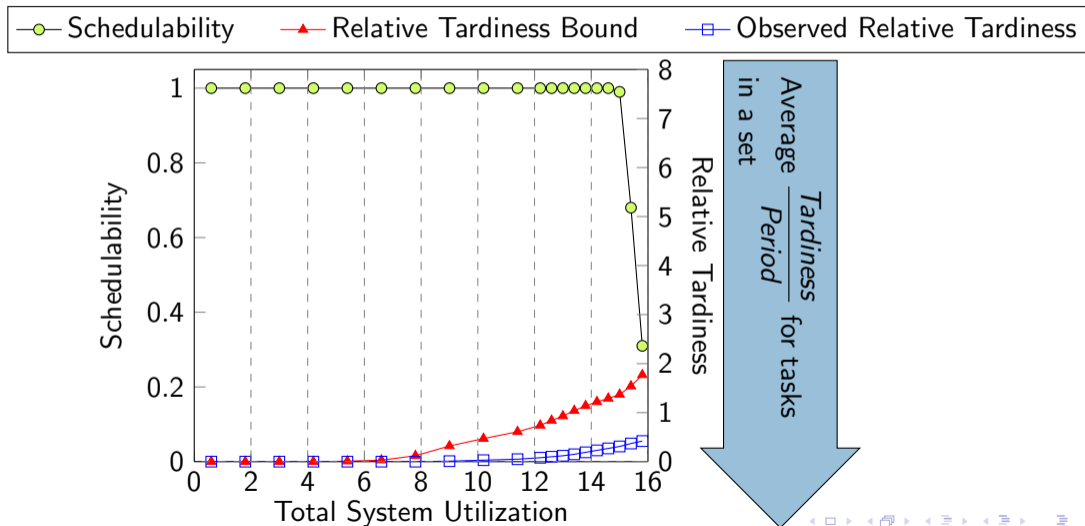
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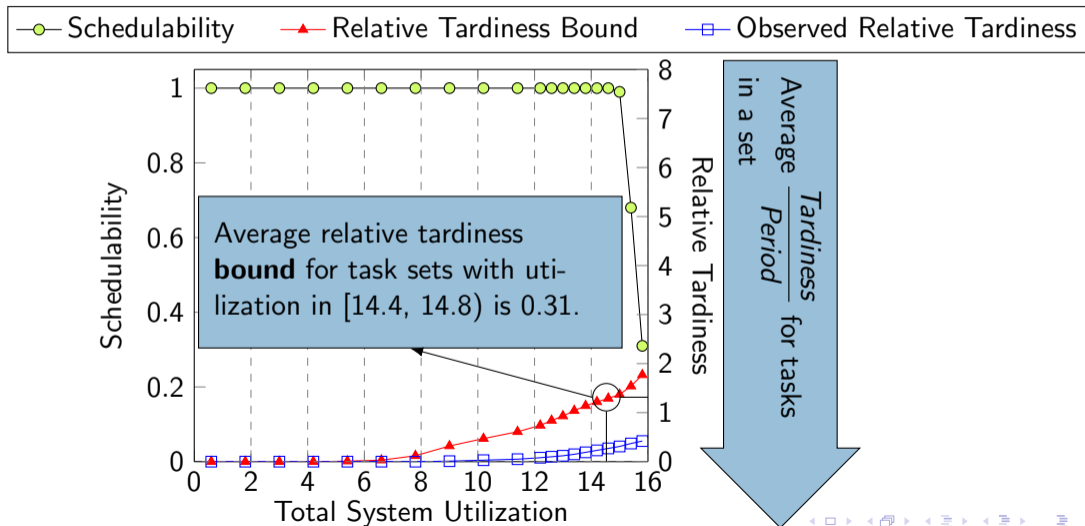


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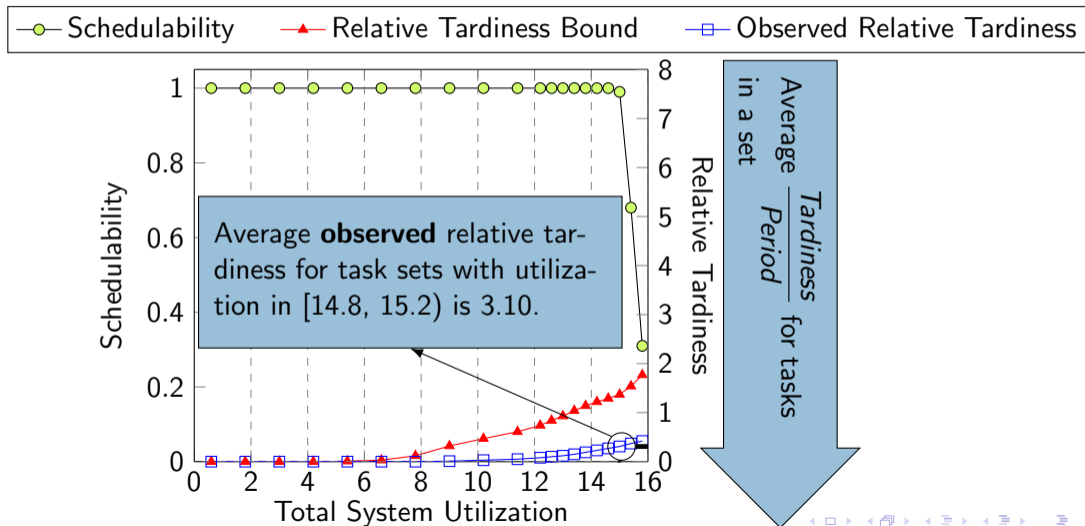




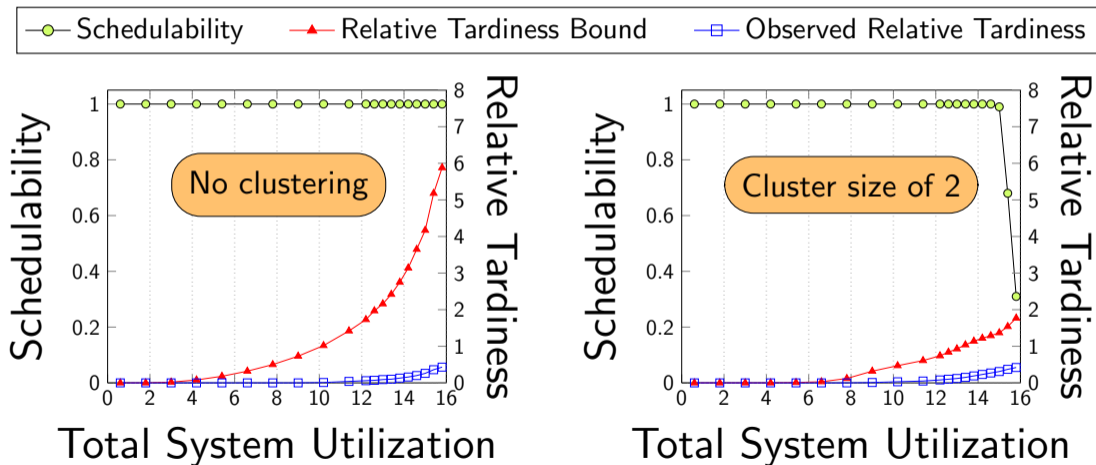
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Thank you for listening.